Peilin Li¹, Xueying Man², Dongmeng Zhu², Tingting Jiang²,

Junhui Tang², Hongmei Xie²

¹Qianshao Farm of Jiansanjiang Administration, Heilongjiang Province, China;

²College of Science, Heilongjiang Bayi Agricultural University, Daqing, 163319, China.

Abstract

Soil fertility is the basic premise of crop yield guarantee, and the main indexes of soil fertility are organic matter, total nitrogen, hydrolyzed nitrogen, rapidly available potassium, slowly available potassium, available phosphorus, total phosphorus, etc. In the face of the severe challenge of soil degradation, it has become the primary task to accurately evaluate soil fertility to achieve the goal of sustainable agricultural development. Based on the main indexes of soil fertility, this paper firstly established a comprehensive evaluation model with principal component analysis method to evaluate the soil fertility at each point of outpost farm, constructed a comprehensive evaluation function F, and obtained the comprehensive evaluation results. Secondly, the comprehensive evaluation model of grey correlation analysis was used to evaluate soil fertility, and the evaluation results were generally consistent with the actual results. The grey correlation curve is used to analyze the close degree of each index, which further proves the rationality of the evaluation index selected in this paper.

Keywords

Soil fertility; Principal factor analysis; Grey relation analysis; SPSS.

1. Introduction

Soil fertility is related to crop yield, and soil fertility of different degrees is crucial to crop yield and quality. In order to ensure sustainable development of agriculture, it is essential to evaluate soil fertility scientifically and effectively. Meanwhile, the evaluation of soil fertility is conducive to land resource utilization, scientific fertilization, crop layout adjustment and land development and consolidation.

In 2004, J.L et al. comprehensively considered the factors affecting soil fertility, such as plant crop species, rainfall, and season, and comprehensively studied and analyzed soil fertility by comprehensively using rainfall sequences at different time periods and NDVI. Dhaeze studies the suitability of land for different USES under certain conditions based on the requirements of soil fertility and socio-economic factors in agricultural policy making. In 2007, Gonzalez used geographic information technology to analyze in detail the changes of farmland plot size in recent years, and finally concluded that the effects of soil fertility changes on soil productivity.

Cao Chengmian et al. had a sudden idea for the first time to obtain the weight in the mean sum through the correlation between the indexes of fertility index content, thus the evaluation of soil fertility by the numerical comprehensive evaluation model became a reality. Wu Wei et al. adopted the fuzzy mathematical model and assigned the corresponding membership degree to the selected indicators, so that the evaluation value could well reflect the correlation between the indicators and the evaluation level of the indicators themselves, and could accurately evaluate the fertility quality of the research area. Liu Changwen et al. selected 4 evaluation indexes in the research area and used multivariate statistical analysis method to evaluate soil fertility, and obtained a conclusion that was as high as 80% consistent with the reality. It reflected that soil physical characteristics were inextricably linked with crop yield and at the same time reduced the unreasonable influence brought by other factors. Zhong Jihong et al. used numerical comprehensive evaluation method to analyze and study the soil fertility quality evaluation of forest lateritic soil. The BP neural network method proposed by Han Lei et al. established a comprehensive evaluation model of soil fertility in Ansai County, which not only compared the level of soil fertility but also visually identified the classification of soil fertility. In the soil fertility evaluation of Xi 'an Vegetable district, Wang Jing et al. firstly calculated their respective weights, supported by corresponding models, and then summarized them to obtain the comprehensive evaluation cloud model of soil fertility evaluation results.

2. Preliminary knowledge

Qianshao Farm, one of the world's three black soil belt, is a natural cradle for rice production and has been awarded the title of "The first Farm reclamation in the East". In this paper, 7 indexes related to outpost farm soil in 2017 were selected to study soil fertility.

Principal component analysis (PCA) : In the analysis of multi-indicator problems, considering that the information presented by multiple indicators may be overlapped and that multiple indicators may involve distribution rules in various aspects, we need to reduce the difficulty of operation and improve work efficiency in order to avoid the problem becoming complicated. In the case of little information loss, it is necessary to use the dimensionality reduction idea of principal component to reduce multiple indicators to several representative comprehensive indicators. It is for this reason that the principal component is more advantageous than the original data in some aspects.

Grey relational analysis: Grey relational analysis suggests that the similarity of the geometric shapes of sequence curves can be used to determine whether the objects are closely related to each other. The closer the curves are, the greater the correlation between the corresponding sequences is, and vice versa. Therefore, grey relational degree analysis provides a quantitative measure of development and change situation, which is very suitable for dynamic process analysis. First, the data sequence and the standard data sequence are determined, then the data is initialized, and finally the grey correlation coefficient between the evaluation factors is calculated.

Selection of indexes: The evaluation indexes of soil fertility must have scientific basis, and the evaluation indexes play a decisive role in the evaluation of soil fertility. According to the quality of agricultural land grading procedures "(GB/T28407-2012) and the second national soil survey classification standard of the nutrients in the pressure in the process of sand to the soil fertility evaluation, finally determined the soil organic matter, total nitrogen, total potassium and total phosphorus, available phosphorus and available potassium, hydrolysis nitrogen the seven indicators as a contestant factor of soil integrated fertility evaluation.

3. Establishment and Solution of soil fertility evaluation model

3.1 Principal component analysis evaluation model

The contents of organic matter, total nitrogen, total phosphorus, total potassium, hydrolyzed nitrogen, available phosphorus and available potassium in soil were determined by different methods.

| The evaluation index | Variable symbol |
|--------------------------|-----------------|
| The organic matter | OM |
| Total nitrogen | TN |
| Hydrolysis nitrogen | WN |
| The effective phosphorus | AP |
| Available k | AK |
| Total phosphorus | TP |
| Total potassium | SK |

Table 3-1 rice quality evaluation index system table

Standardize the original data and conduct correlation test. The test results are shown in the table 3-2.

| KMO and Bartlett I | | | | | |
|-----------------------------|-------------------------------|---------|--|--|--|
| Sample enough Kaiser-Mey | yer-OlkinTo measure the 0.663 | | | | |
| | The approximate chi-square | 338.463 | | | |
| Bartlett Test of sphericity | df | 21 | | | |
| | Sig. | 0.05 | | | |

Table3-2 KMO and Bartlett's test table

As shown in Table 3-2, Correlation is equal to 0.663>0.5, Therefore, principal component analysis is applicable.

Calculate the correlation coefficient matrix and the cumulative contribution rate:

| | | | Correlat | ion coefficien | t matrix | | | |
|---------|----|--------|----------|----------------|----------|-------|-------|----|
| | | OM | TN | WN | AK | SK | AP | TP |
| | OM | 1 | | | | | | |
| | TN | 0.152 | 1 | | | | | |
| | WN | 0.301 | -0.086 | 1 | | | | |
| related | AK | 0.320 | -0.024 | 0.209 | 1 | | | |
| | SK | -0.192 | -0.074 | -0.044 | -0.099 | 1 | | |
| | AP | -0.198 | 0.115 | -0.310 | -0.203 | 0.045 | 1 | |
| | ТР | 0.244 | -0.114 | -0.097 | 0.458 | 0.069 | 0.364 | 1 |

Table 3-3 correlation coefficient matrix table

Table 3-4 Cumulative contribution rate

| The principal components | The eigenvalue | contribution | Cumulative contribution rate |
|--------------------------|----------------|--------------|------------------------------|
| 1 | 1.933 | 42.646 | 42.646 |
| 2 | 1.586 | 34.547 | 77.193 |
| 3 | 1.181 | 10.061 | 87.254 |
| 4 | 1.018 | 9.032 | 95.286 |

According to Table 3-4, when there are 4 principal components, the cumulative contribution rate in the table is 95.286%, which meets the relevant requirements. Therefore, only 4 principal components are needed to accurately express the main conditions of soil fertility.

Calculate the corresponding eigenvectors of each principal component,

| T1 | T2 | T3 | T4 |
|--------|--------|--------|--------|
| 0.377 | -0.380 | 0.361 | 0.623 |
| -0.060 | 0.625 | 0.747 | 0.546 |
| 0.382 | 0.096 | -0.202 | -0.346 |
| 0.353 | -0.048 | 0.267 | -0.122 |
| 0.024 | 0.446 | -0.158 | 0.099 |
| 0.348 | 0.733 | 0.387 | -0.044 |
| 0.439 | -0.072 | 0.710 | 0.012 |

Table 3-5 The eigenvectors of the principal components

According to Table 3-5, the following linear regression equation can be obtained:

$$\begin{split} Z_1 &= 0.377 * \text{OM} - 0.060 * \text{TN} + 0.382 * \text{WN} + 0.353 * \text{AK} \\ &+ 0.024 * \text{SK} + 0.348 * \text{AP} + 0.439 * \text{TP} \\ Z_2 &= -0.380 * \text{OM} + 0.625 * \text{TN} + 0.096 * \text{WN} - 0.048 * \text{AK} \\ &+ 0.446 * \text{SK} + 0.733 * \text{AP} - 0.072 * \text{TP} \\ Z_3 &= 0.361 * \text{OM} + 0.747 * \text{TN} - 0.202 * \text{WN} + 0.267 * \text{AK} \\ &- 0.158 * \text{SK} + 0.387 * \text{AP} + 0.710 * \text{TP} \\ Z_4 &= 0.623 * \text{OM} + 0.546 * \text{TN} - 0.346 * \text{WN} - 0.122 * \text{AK} \\ &+ 0.099 * \text{SK} - 0.044 * \text{AP} + 0.012 * \text{TP} \end{split}$$

By using the eigenvalues obtained from principal components, the weights of each component are obtained, and then the comprehensive evaluation function is written to show its relationship with each principal component Z_i (i = 1, 2, 3, 4) linear function of:

$$F = 0.391 * Z_1 + 0.294 * Z_2 + 0.198 * Z_3 + 0.117 * Z_4$$

| The principal components | The eigenvalue | Characteristic root weight | | |
|--------------------------|----------------|----------------------------|--|--|
| Z1 | 2.487 | 0.391 | | |
| Z2 | 1.396 | 0.294 | | |
| Z3 | 1.003 | 0.198 | | |
| Z4 | 0.782 | 0.117 | | |

Table 3-6 The eigenvalue corresponding to the principal component

The principal component is known Z_i (i = 1, 2, 3, 4), and each index factor OM, TN, WN the linear relationship between the comprehensive index function F and each evaluation index OM, TN, WN, etc., as well as the ranking of each index factor, see table 3-7.

| Index factors | Index coefficient in comprehensive evaluation function | The ranking of influencing factors in the comprehensive evaluation index function |
|-------------------------------|--|---|
| The organic matter (OM) | 0.061 | 6 |
| Total nitrogen (TN) | 0.198 | 3 |
| Total phosphorus (TP) | 0.279 | 2 |
| Total potassium (AK) | 0.129 | 5 |
| Hydrolysis nitrogen (WN) | 0.118 | 4 |
| The effective phosphorus (AP) | 0.280 | 1 |
| Available k (SK) | 0.153 | 7 |

The comprehensive evaluation function model based on principal component analysis is:

F

$$= 0.061 * OM + 0.198 * TN + 0.279 * TP + 0.129 * AK$$

| Sample area | Y1 | Y2 | Y3 | Y4 | Y5 | Y6 | Y7 | Y8 | Y9 | Y10 |
|-------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| score | -0.403 | -0.736 | -0.498 | 1.041 | -0.387 | -0.278 | 0.672 | 0.425 | 1.601 | 1.785 |
| The sorting | 22 | 27 | 24 | 3 | 21 | 19 | 5 | 9 | 2 | 1 |
| Sample area | Y11 | Y12 | Y13 | Y14 | Y15 | Y16 | Y17 | Y18 | Y19 | Y20 |
| score | 0.386 | -0.141 | 0.538 | 0.619 | 0.135 | -0.128 | 0.712 | -0.015 | 0.549 | -0.427 |
| The sorting | 10 | 17 | 8 | 6 | 11 | 16 | 4 | 14 | 7 | 23 |
| Sample area | Y21 | Y22 | Y23 | Y24 | Y25 | Y26 | Y27 | Y28 | Y29 | Y30 |
| score | -0.101 | -0.853 | -0.594 | -0.601 | -0.288 | -0.816 | -0.739 | 0.071 | -0.246 | 0.102 |
| The sorting | 15 | 30 | 25 | 26 | 20 | 29 | 28 | 13 | 18 | 12 |

In the soil fertility score of the various test plots, the score of many test plots is negative, but it does not mean that the soil fertility score of the test plots is negative. The positive and negative values here only represent the location relationship between the sample plot and the average level, and the average level of soil fertility is counted as zero, which is the result of data standardization in the evaluation process.

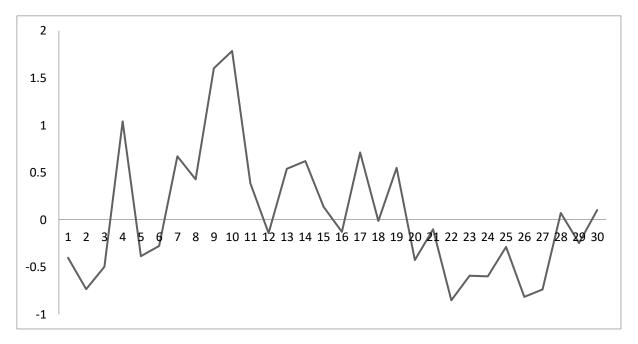


Figure3-1 Trend chart of soil fertility by principal component analysis

As can be seen from Figure 3-1, although the overall trend is that soil fertility first increases and then decreases, soil fertility in many test plots is inconsistent with the change trend. The evaluation model based on principal component analysis (PCA) is applied to the study of soil fertility in this paper, and the evaluation results obtained do not reach a high accuracy rate.

In the process of building a mathematical model based on principal component analysis, a quantifiable ranking of relative importance is obtained for the seven evaluation indexes selected. In this way, we can understand the main factors affecting soil fertility and provide practical guidance for improving soil fertility.

3.2 Grey relational analysis evaluation model

The decision matrix X is composed of 31 sample plots, real side values of 7 evaluation indexes and reference sequence.

| | ОМ | TN | WN | AK | SK | AP | ТР |
|-----|-------|-------|-------|-----|-----|-------|-------|
| Y1 | 60.67 | 1.14 | 355 | 234 | 311 | 11.85 | 1.206 |
| Y2 | 71.38 | 1.32 | 266.1 | 197 | 348 | 8.89 | 1.26 |
| Y3 | 59.9 | 1.47 | 249.1 | 370 | 348 | 14.49 | 1.059 |
| Y4 | 47.89 | 1.25 | 336.9 | 240 | 330 | 16.71 | 1.299 |
| Y5 | 58.74 | 1.65 | 228.9 | 467 | 268 | 9.15 | 1.296 |
| Y6 | 76.57 | 1.05 | 265.3 | 429 | 266 | 16.52 | 1.263 |
| Y7 | 74.79 | 1.33 | 248.5 | 335 | 320 | 14.42 | 1.327 |
| Y8 | 74.78 | 1.52 | 139.6 | 239 | 324 | 6.72 | 1.293 |
| Y9 | 51.87 | 1.42 | 156.6 | 165 | 347 | 6.81 | 1.283 |
| Y10 | 67.67 | 1.44 | 150.9 | 312 | 360 | 5.79 | 1.287 |
| Y11 | 56.97 | 1.46 | 198.8 | 180 | 536 | 6.72 | 1.447 |
| Y12 | 51.93 | 1.47 | 325.3 | 222 | 518 | 13.42 | 1.141 |
| Y13 | 50.76 | 1.15 | 225.9 | 126 | 501 | 21.68 | 1.03 |
| Y14 | 55.55 | 1.392 | 334.9 | 293 | 454 | 20.67 | 1.31 |
| Y15 | 49.12 | 1.447 | 368.6 | 366 | 450 | 21.19 | 1.308 |
| Y16 | 73.45 | 1.243 | 355.1 | 340 | 383 | 20.91 | 1.316 |
| Y17 | 50.82 | 1.15 | 375.3 | 373 | 381 | 16.15 | 1.243 |
| Y18 | 55.57 | 1.24 | 219.9 | 381 | 345 | 6.25 | 1.21 |
| Y19 | 54.02 | 1.24 | 296.6 | 244 | 359 | 9.01 | 1.319 |
| Y20 | 54.79 | 1.55 | 349.7 | 317 | 351 | 9.05 | 1.142 |
| Y21 | 55.88 | 1.31 | 218.7 | 419 | 369 | 9.87 | 1.311 |
| Y22 | 52.75 | 1.25 | 199.7 | 296 | 330 | 6.74 | 1.305 |
| Y23 | 45.84 | 1.33 | 287.4 | 226 | 329 | 7.42 | 1.256 |
| Y24 | 40.54 | 1.31 | 297.9 | 201 | 315 | 23.43 | 1.268 |
| Y25 | 40.01 | 1.44 | 177.5 | 176 | 369 | 7.86 | 1.379 |
| Y26 | 37.12 | 1.55 | 171.2 | 145 | 363 | 4.41 | 1.173 |
| Y27 | 36.3 | 1.4 | 315.4 | 208 | 355 | 12.37 | 1.213 |
| Y28 | 32.55 | 1.412 | 258.7 | 136 | 346 | 6.74 | 1.254 |
| Y29 | 47.66 | 1.25 | 245.4 | 115 | 353 | 30.4 | 1.11 |

Table 3-9 Decision matrix value

Standardize the data and apply transformations

$$\begin{split} f &: Y \to Z \\ Z_i(k) &= \frac{Y_i(k)}{Y_0(k)} \, (i \, = \, 0, \, 2, \, ..., \, n) (k \, = \, 1, \, 2, \, ..., \, m) \end{split}$$

Get the matrix Y, and organize into a data table 3-10:

| | Organic matter mass fraction | Total nitrogen mass fraction | Totalphos phorus mass fraction | Totalpota ssium mass fraction | Hydrolyze d nitrogen mass fraction | Availab le p mass fraction | Mass fraction of available potassium |
|-----|---------------------------------------|---------------------------------------|---|--|---|-------------------------------------|---|
| Y1 | 0.765 | 0.579 | 0.750 | 0.842 | 0.897 | 0.750 | 0.776 |
| Y2 | 0.839 | 0.636 | 0.936 | 0.878 | 0.965 | 0.992 | 0.840 |
| Y3 | 0.799 | 0.850 | 0.689 | 0.649 | 0.948 | 0.532 | 0.663 |
| Y4 | 0.827 | 0.732 | 0.679 | 0.946 | 0.812 | 0.548 | 0.998 |
| Y5 | 0.304 | 0.636 | 0.902 | 0.919 | 0.993 | 0.805 | 0.975 |
| Y6 | 0.977 | 0.667 | 0.937 | 0.781 | 0.752 | 0.873 | 0.673 |
| Y7 | 0.995 | 0.857 | 0.562 | 0.713 | 0.825 | 0.466 | 0.974 |
| Y8 | 0.694 | 0.934 | 0.777 | 0.690 | 0.710 | 0.929 | 0.992 |
| Y9 | 0.405 | 0.845 | 0.964 | 0.891 | 0.746 | 0.850 | 0.769 |
| Y10 | 0.842 | 0.889 | 0.743 | 0.577 | 0.889 | 0.606 | 0.878 |
| Y11 | 0.912 | 0.849 | 0.636 | 0.873 | 0.966 | 0.997 | 0.789 |
| Y12 | 0.977 | 0.782 | 0.694 | 0.568 | 0.967 | 0.615 | 0.903 |
| Y13 | 0.494 | 0.826 | 0.825 | 0.540 | 0.906 | 0.953 | 0.184 |
| Y14 | 0.884 | 0.951 | 0.627 | 0.915 | 0.991 | 0.516 | 0.998 |
| Y15 | 0.495 | 0.859 | 0.963 | 0.929 | 0.851 | 0.987 | 0.795 |
| Y16 | 0.692 | 0.925 | 0.689 | 0.971 | 0.995 | 0.772 | 0.945 |
| Y17 | 0.935 | 0.783 | 0.586 | 0.772 | 0.906 | 0.387 | 0.973 |
| Y18 | 0.972 | 0.795 | 0.879 | 0.640 | 0.580 | 0.944 | 0.901 |
| Y19 | 0.425 | 0.785 | 0.790 | 0.918 | 0.978 | 0.951 | 0.866 |
| Y20 | 0.989 | 0.845 | 0.625 | 0.767 | 0.821 | 0.906 | 0.986 |
| Y21 | 0.944 | 0.954 | 0.913 | 0.706 | 0.894 | 0.683 | 0.995 |
| Y22 | 0.869 | 0.973 | 0.874 | 0.764 | 0.997 | 0.890 | 0.962 |
| Y23 | 0.884 | 0.985 | 0.653 | 0.889 | 0.957 | 0.768 | 0.955 |
| Y24 | 0.987 | 0.992 | 0.596 | 0.876 | 0.714 | 0.335 | 0.875 |
| Y25 | 0.928 | 0.764 | 0.965 | 0.824 | 0.984 | 0.561 | 0.851 |
| Y26 | 0.978 | 0.903 | 0.842 | 0.434 | 0.978 | 0.805 | 0.968 |
| Y27 | 0.897 | 0.857 | 0.820 | 0.654 | 0.975 | 0.545 | 0.338 |
| Y28 | 0.464 | 0.885 | 0.949 | 0.846 | 0.873 | 0.451 | 0.885 |
| Y29 | 0.435 | 0.876 | 0.684 | 0.764 | 0.692 | 0.513 | 0.432 |
| Y20 | 0.543 | 0.769 | 0.620 | 0.961 | 0.394 | 0.346 | 0.396 |

Table 3-10 The indicators are digitized

According to the formula

$$V_{i}(k) = |y_{0}(k) - y_{i}(k)| (i = 1, 2, ..., n) (k = 1, 2, ..., m)$$

The absolute difference sequence is calculated $\Box(k)$, see table 3-11.

| | | 14010 5 11 | i bequence (| | merenees | | |
|-----|-------|------------|--------------|-------|----------|-------|-------|
| Δ1 | 0.185 | 0.429 | 0.365 | 0.410 | 0.276 | 0.587 | 0.532 |
| Δ2 | 0.278 | 0.599 | 0.418 | 0.242 | 0.184 | 0.548 | 0.577 |
| Δ3 | 0.433 | 0.415 | 0.125 | 0.239 | 0.316 | 0.248 | 0.403 |
| Δ4 | 0.124 | 0.578 | 0.325 | 0.346 | 0.485 | 0.654 | 0.465 |
| Δ5 | 0.127 | 0.174 | 0.004 | 0.263 | 0.276 | 0.546 | 0.434 |
| Δ6 | 0.145 | 0.616 | 0.178 | 0.064 | 0.264 | 0.545 | 0.038 |
| Δ7 | 0.121 | 0.201 | 0.023 | 0.045 | 0.230 | 0.541 | 0.096 |
| Δ8 | 0.295 | 0.268 | 0.369 | 0.155 | 0.002 | 0.015 | 0.293 |
| Δ9 | 0.194 | 0.399 | 0.473 | 0.368 | 0.376 | 0.487 | 0.432 |
| Δ10 | 0.179 | 0.549 | 0.335 | 0.348 | 0.284 | 0.448 | 0.319 |
| Δ11 | 0.443 | 0.424 | 0.525 | 0.636 | 0.320 | 0.340 | 0.036 |
| Δ12 | 0.123 | 0.538 | 0.385 | 0.326 | 0.425 | 0.754 | 0.467 |
| Δ13 | 0.147 | 0.274 | 0.024 | 0.463 | 0.676 | 0.366 | 0.234 |
| Δ14 | 0.267 | 0.526 | 0.238 | 0.191 | 0.464 | 0.547 | 0.438 |
| Δ15 | 0.481 | 0.291 | 0.469 | 0.040 | 0.243 | 0.543 | 0.016 |
| Δ16 | 0.395 | 0.318 | 0.378 | 0.025 | 0.495 | 0.019 | 0.299 |
| Δ17 | 0.186 | 0.439 | 0.345 | 0.468 | 0.260 | 0.587 | 0.562 |
| Δ18 | 0.478 | 0.419 | 0.635 | 0.247 | 0.384 | 0.580 | 0.540 |
| Δ19 | 0.452 | 0.301 | 0.409 | 0.236 | 0.330 | 0.248 | 0.436 |
| Δ20 | 0.324 | 0.442 | 0.386 | 0.336 | 0.685 | 0.654 | 0.435 |
| Δ21 | 0.128 | 0.172 | 0.294 | 0.664 | 0.270 | 0.546 | 0.462 |
| Δ22 | 0.165 | 0.613 | 0.358 | 0.564 | 0.460 | 0.496 | 0.498 |
| Δ23 | 0.181 | 0.211 | 0.423 | 0.445 | 0.643 | 0.367 | 0.656 |
| Δ24 | 0.245 | 0.349 | 0.471 | 0.381 | 0.042 | 0.095 | 0.203 |
| Δ25 | 0.199 | 0.449 | 0.355 | 0.568 | 0.373 | 0.597 | 0.472 |
| Δ26 | 0.288 | 0.559 | 0.461 | 0.398 | 0.249 | 0.447 | 0.648 |
| Δ27 | 0.451 | 0.405 | 0.484 | 0.246 | 0.323 | 0.258 | 0.466 |
| Δ28 | 0.129 | 0.479 | 0.331 | 0.306 | 0.499 | 0.634 | 0.565 |
| Δ29 | 0.177 | 0.277 | 0.044 | 0.404 | 0.396 | 0.566 | 0.454 |
| Δ30 | 0.475 | 0.626 | 0.408 | 0.164 | 0.364 | 0.483 | 0.058 |

Table 3-11 Sequence of absolute differences

$$r_{ij} = \frac{\min_{m} \min_{n} \left| V_{i}(k) \right| + \rho \max_{m} \max_{m} \left| V_{i}(k) \right|}{\left| V_{i}(k) + \rho \max_{m} \max_{n} \left| V_{j}(k) \right| \right|}$$

then form evaluation matrix R.

| 0.675 | 0.468 | 0.513 | 0.474 | 0.579 | 0.363 | 0.424 |
|-------|-------|-------|-------|-------|-------|-------|
| 0.565 | 0.387 | 0.48 | 0.622 | 0.704 | 0.379 | 0.392 |
| 0.484 | 0.47 | 0.989 | 0.841 | 0.651 | 0.583 | 0.456 |
| 0.78 | 0.387 | 0.635 | 0.896 | 0.557 | 0.384 | 0.441 |
| 0.68 | 0.667 | 0.978 | 0.564 | 0.573 | 0.402 | 0.475 |
| 0.701 | 0.384 | 0.684 | 0.849 | 0.588 | 0.409 | 0.916 |
| 0.764 | 0.657 | 0.938 | 0.92 | 0.657 | 0.403 | 0.959 |
| 0.561 | 0.571 | 0.5 | 0.949 | 1 | 0.96 | 0.566 |
| 0.883 | 0.432 | 0.674 | 0.697 | 0.594 | 0.419 | 0.63 |
| 0.721 | 0.502 | 0.582 | 0.768 | 0.711 | 0.457 | 0.482 |
| 0.8 | 0.711 | 0.464 | 0.709 | 0.63 | 0.471 | 0.542 |
| 0.736 | 0.393 | 0.542 | 0.974 | 0.612 | 0.414 | 0.623 |
| 0.419 | 0.654 | 0.472 | 0.489 | 0.599 | 0.35 | 0.484 |
| 0.503 | 0.908 | 0.548 | 0.752 | 0.564 | 0.408 | 0.654 |
| 0.936 | 0.646 | 0.522 | 0.596 | 0.619 | 0.373 | 0.414 |
| 0.429 | 0.482 | 0.489 | 0.464 | 0.651 | 0.366 | 0.384 |
| 0.522 | 0.51 | 0.563 | 0.593 | 0.675 | 0.342 | 0.404 |
| 0.522 | 0.511 | 0.566 | 0.597 | 0.562 | 0.346 | 0.512 |
| 0.791 | 0.531 | 0.499 | 0.592 | 0.56 | 0.347 | 0.519 |
| 0.385 | 0.717 | 0.551 | 0.583 | 0.626 | 0.367 | 0.417 |
| 0.497 | 0.56 | 0.508 | 0.452 | 0.736 | 0.381 | 0.43 |
| 0.509 | 0.422 | 0.491 | 0.793 | 0.676 | 0.351 | 0.483 |
| 0.478 | 0.473 | 0.539 | 0.576 | 0.627 | 0.376 | 0.534 |
| 0.483 | 0.653 | 0.527 | 0.743 | 0.595 | 0.45 | 0.609 |
| 0.654 | 0.68 | 0.497 | 0.532 | 0.732 | 0.399 | 0.408 |
| 0.652 | 0.481 | 0.526 | 0.887 | 0.531 | 0.425 | 0.439 |
| 0.539 | 0.443 | 0.478 | 0.52 | 0.57 | 0.357 | 0.412 |
| 0.839 | 0.377 | 0.499 | 0.646 | 0.672 | 0.36 | 0.462 |
| 0.701 | 0.413 | 0.517 | 0.492 | 0.684 | 0.363 | 0.454 |
| 0.511 | 0.439 | 0.488 | 0.646 | 0.619 | 0.334 | 0.437 |
| | | | | | | |

Table 3-11 The evaluation matrix

Because different indexes have different influences on soil quality, corresponding weight coefficients should be assigned to different indexes in the evaluation process, and the weight matrix should be obtained by AHP:

 $W^{T} = (0.076 \ 0.053 \ 0.037 \ 0.071 \ 0.540 \ 0.089 \ 0.078)$

According to the formula

$$r(y_0, y_i) = \sum_{j=1}^{m} r_{ij} w_j (i = 1, 2, ..., n)$$

The grey relational degree of each index in the reference plot was calculated

| Sample area | Y1 | Y2 | Y3 | Y4 | Y5 | Y6 | Y7 | Y8 | Y9 | Y10 |
|-------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| score | 0.503 | 0.636 | 0.598 | 0.517 | 0.587 | 0.578 | 0.672 | 0.525 | 0.601 | 0.685 |
| The sorting | 22 | 27 | 24 | 3 | 21 | 19 | 5 | 9 | 2 | 1 |
| Sample area | Y11 | Y12 | Y13 | Y14 | Y15 | Y16 | Y17 | Y18 | Y19 | Y20 |
| Score | 0.586 | 0.541 | 0.538 | 0.619 | 0.535 | 0.512 | 0.612 | 0.510 | 0.549 | 0.527 |
| The sorting | 10 | 17 | 8 | 6 | 11 | 16 | 4 | 14 | 7 | 23 |
| Sample area | Y21 | Y22 | Y23 | Y24 | Y25 | Y26 | Y27 | Y28 | Y29 | Y30 |
| Score | 0.511 | 0.698 | 0.594 | 0.601 | 0.528 | 0.506 | 0.689 | 0.571 | 0.546 | 0.502 |
| The sorting | 15 | 30 | 25 | 26 | 20 | 29 | 28 | 13 | 18 | 12 |

Table 3-12 Index coefficient and ranking

Figure 3-2 intuitively shows the change trend of soil fertility associated with gray.

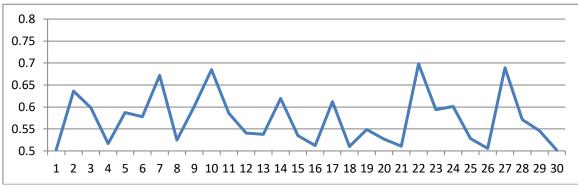


Figure3-2 A gray-related soil fertility trend chart

As can be seen from the figure above, the general trend is that soil fertility first increases and then decreases. The evaluation model based on grey correlation is applied to the study of soil fertility in this paper, and the obtained evaluation results can reach a high accuracy rate.

By comparing the principal component score with the gray correlation score, it can be found that the gray correlation has a better effect than the principal component analysis and is more suitable for the analysis and evaluation of soil fertility.

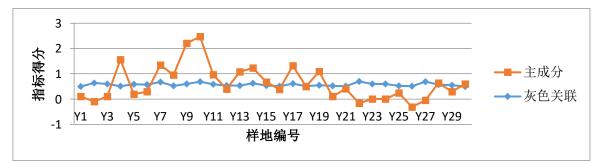


Figure 3-3 Effect comparison

4. Conclusion

In this paper, the evaluation model of grey correlation analysis and the comprehensive evaluation model of principal component analysis were established respectively, and the soil fertility of the outpost farm was comprehensively evaluated. It is found that the evaluation results of the two models are different. During the evaluation process, the standardization of the two evaluation methods is

inconsistent, which leads to the slight difference of the evaluation results. Firstly, the comprehensive evaluation model of principal component analysis was used to evaluate soil fertility. In addition, the influence degree of each evaluation index on soil fertility was ranked from small to large as: available potassium, organic matter, hydrolyzed nitrogen, total potassium, total phosphorus, available phosphorus, and total nitrogen. Based on the principal component analysis (PCA) comprehensive evaluation model, the comprehensive soil fertility score of each outpost farm can be clearly seen. Secondly, the comprehensive evaluation model of gray correlation analysis is used to evaluate each outpost farm. The data showed that gray correlation was a better indicator of soil fertility than principal component analysis.

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